

AI Planning

2. Planning Formalisms

How to Describe Problems, and What is a “Problem” Anyway?

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Agenda

- 1 Introduction
- 2 Transition Systems
- 3 STRIPS Planning
- 4 Finite-Domain Representation (FDR) Planning
- 5 STRIPS vs. FDR
- 6 Extended Planning Frameworks [for Reference]
- 7 Conclusion

Reminder: Planning = General Problem Solving

(some new problem)



describe problem in planning language \mapsto use off-the-shelf solver



(its solution)

- Any problem that can be formulated as a **planning problem**.
- Don't write the C++ code, just describe the problem!
- Don't maintain the C++ code, maintain the description!

What is a Planning Problem?

Given a **planning task**:

- A description of the **initial state**.
- A description of the **goal condition**.
- A description of a set of **possible actions**.

→ Find a schedule of actions (a **plan**) that brings us from the initial state to a state in which the goal condition holds.

Classical Planning

... makes **Simplifying Assumptions**:

- Initial situation unique and completely known, environment deterministic, static, discrete, single-agent.
- Actions executed one-by-one, plans are sequences.

This is often not the case in practice! Examples? Handling uncertainty (robot control), temporal/parallel execution (transportation), ...

So why do we do this?

- Clean framework to study planning problems. (Simplicity is a virtue!)
- Most influential ideas were conceived there. → **This course!**
- Successful applications using classical planning. → **Chapter 4**
- We can successfully **compile** many extended paradigms into classical planning. → **Outlined later in this Chapter**

→ We focus entirely on classical planning in this course.

Algorithmic Problems in Planning

Satisficing Planning

Input: A planning task Π .

Output: A plan for Π , or **unsolvable** if no plan for Π exists.

Optimal Planning

Input: A planning task Π .

Output: An optimal plan for Π , or **unsolvable** if no plan for Π exists.

→ The techniques successful for either one of these are almost disjoint!

→ Satisficing planning is *much* more effective in practice.

→ Programs solving these problems are called (optimal) **planners**, **planning systems**, or **planning tools**.

Computational Complexity in Planning

Why? From this course's point of view, it's simply one technical tool we need.

→ To get a heuristic h , we map the planning problem into a simpler (abstract/relaxed) planning problem, from whose solution we compute h . To compute h efficiently, the “simpler” problem must be solvable in polynomial time.

Definition (PlanEx and PlanOpt). *PlanEx* is the problem of deciding, given a (STRIPS or FDR) planning task Π , *whether or not there exists a plan for Π* . *PlanOpt* is the problem of deciding, given Π and $B \in \mathbb{R}_0^+$, *whether or not there exists a plan for Π whose cost is at most B* .

→ PlanEx \approx satisficing planning, PlanOpt \approx optimal planning.

Theorem (Planning is Hard). *Each of PlanEx and PlanOpt is PSPACE-complete.*

Proof. See Al'18.

Our Agenda for This Chapter

- ② **Transition Systems:** The basic framework we'll be moving in; forms the basis for both STRIPS and FDR. (= state space, cf. AI'18)
- ③ **STRIPS Planning:** STRIPS is by far the most wide-spread planning formalism. It is also the simplest possible reasonably expressive planning formalism, and thus a canonical subject to study.
- ④ **Finite-Domain Representations (FDR):** FDR is only slightly more general than STRIPS, but as we shall see can be quite useful.
- ⑤ **STRIPS vs. FDR:** The two formalisms can be compiled into each other. Such compilations are wide-spread in practice, and we will use them at some points during the course.
- ⑥ **Extended Planning Frameworks:** To at least give you a brief glimpse beyond classical planning.

Transition Systems

→ State space of planning task = a transition system.

Definition (Transition System). A *transition system* is a 6-tuple

$\Theta = (S, L, c, T, I, S^G)$ where:

- S is a finite set of *states*.
- L is a finite set of transition *labels*.
- $c : L \mapsto \mathbb{R}_0^+$ is the *cost function*.
- $T \subseteq S \times L \times S$ is the *transition relation*.
- $I \in S$ is the *initial state*.
- $S^G \subseteq S$ is the set of *goal states*.

The *size* of Θ is its number of states, $\text{size}(\Theta) := |S|$.

We say that Θ *has the transition* (s, l, s') if $(s, l, s') \in T$. We also write this $s \xrightarrow{l} s'$, or $s \rightarrow s'$ when not interested in l .

We say that Θ is *deterministic* if, for all states s and labels l , there is at most one state s' with $s \xrightarrow{l} s'$.

We say that Θ has *unit costs* if, for all $l \in L$, $c(l) = 1$.

Transition Systems, ctd.

Terminology: $\Theta = (S, A, c, T, I, S^G)$; $s, s', s_i \in S$

- s' **successor** of s if $s \rightarrow s'$; s **predecessor** of s' if $s \rightarrow s'$.
- s' **reachable** from s if there exists a sequence of transitions:

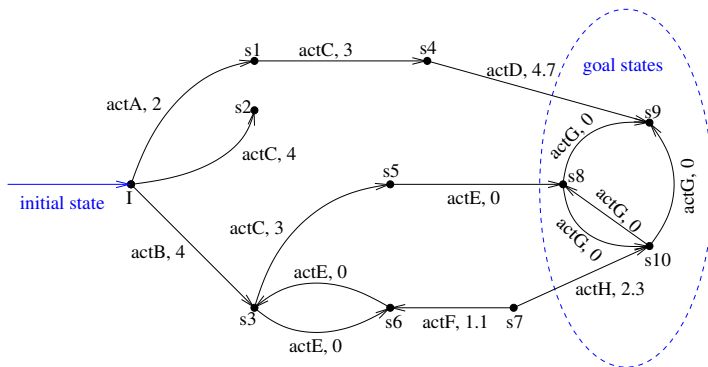
$$s = s_0 \xrightarrow{l_1} s_1, \dots, s_{n-1} \xrightarrow{l_n} s_n = s'$$

- $n = 0$ possible; then $s = s'$.
- l_1, \dots, l_n is called **path** from s to s' .
- s_0, \dots, s_n is also called **path** from s to s' .
- The **cost** of that path is $\sum_{i=1}^n c(l_i)$.
- s' **reachable** (without reference state) means reachable from I .
- **Solution** for s : path from s to some $s' \in S^G$; **optimal** if cost is minimal among all solutions for s .
- s is **solvable** if it has a solution; else, s is a **dead end**.
- Solution for I is called **solution for Θ** ; Θ is **solvable** if it has a solution.

Note: We allow non-deterministic Θ here: In each state s_i , a solution may select any one outgoing transition labeled with l_{i+1} . We will need this only for abstractions (\rightarrow **Chapters 11–13**).

Transition Systems: Illustration

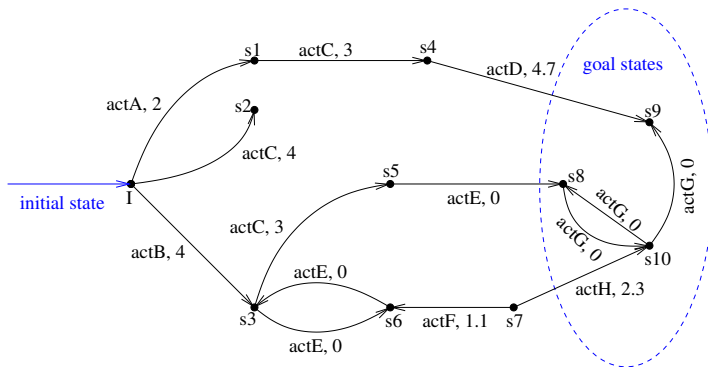
Directed labeled graphs + mark-up for initial state and goal states:



- Are all states in Θ reachable? No: state at bottom, 2nd from right.
- Are all states in Θ solvable? No: state near top, 2nd from left.
- Is this Θ deterministic? No: On two of the goal states, actG labels more than one outgoing transition.

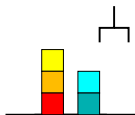
Transition Systems: Illustration, ctd.

Directed labeled graphs + mark-up for initial state and goal states:



- Is this Θ deterministic? Yes.
- What are the optimal solutions for Θ ? Any path that starts with actB, applies actE $n \in \{0, 2, 4, \dots\}$ times, then applies actC then actE and then no action other than actG.

Why don't we simply use Dijkstra? Example Blocksworld



- n blocks, 1 hand.
- A single action either takes a block with the hand or puts a block we're holding onto some other block/the table.

blocks	states	blocks	states
1	1	10	58941091
2	3	11	824073141
3	13	12	12470162233
4	73	13	202976401213
5	501	14	3535017524403
6	4051	15	65573803186921
7	37633	16	1290434218669921
8	394353	17	26846616451246353
9	4596553	18	588633468315403843

→ We are interested in solving **huge** transition systems, represented in a **compact** way as **planning tasks** (up next).

STRIPS Planning: Syntax

Definition (STRIPS Planning Task). A *STRIPS planning task* is a 5-tuple $\Pi = (P, A, c, I, G)$ where:

- P is a finite set of *facts*, also *propositions*.
- A is a finite set of *actions*; each $a \in A$ is a triple $a = (pre_a, add_a, del_a)$ of subsets of P referred to as the action's *precondition*, *add list*, and *delete list* respectively; we require that $add_a \cap del_a = \emptyset$.
- $c : A \mapsto \mathbb{R}_0^+$ is the *cost function*.
- $I \subseteq P$ is the *initial state*.
- $G \subseteq P$ is the *goal*.

We say that Π has *unit costs* if, for all $a \in A$, $c(a) = 1$. We will often give each action $a \in A$ a *name* (a string), and identify a with that name.

Diff to AI'18: The cost function c .

→ What for do we allow 0-cost actions? Negligible cost (e.g. switch light on, take photo with smartphone), asking questions about only one kind of actions (e.g. Mars rover *take-picture* only).

STRIPS Encoding of “TSP” in Australia



- **Propositions** P : $\{at(x), visited(x) \mid x \in \{Sydney, Adelaide, Brisbane, Perth, Darwin\}\}$.
- **Initial state** I : $\{at(Sydney), visited(Sydney)\}$.
- **Goal** G : $\{at(Sydney)\} \cup \{visited(x) \mid x \in \{Sydney, Adelaide, Brisbane, Perth, Darwin\}\}$.
- **Actions** $a \in A$: $drive(x, y)$ where x, y have a road.
 - Precondition** pre_a : $\{at(x)\}$.
 - Add list** add_a : $\{at(y), visited(y)\}$.
 - Delete list** del_a : $\{at(x)\}$.
- **Cost function** c :

$$c(drive(x, y)) = \begin{cases} 1 & \{x, y\} = \{Sydney, Brisbane\} \\ 1.5 & \{x, y\} = \{Sydney, Adelaide\} \\ 3.5 & \{x, y\} = \{Adelaide, Perth\} \\ 4 & \{x, y\} = \{Adelaide, Darwin\} \end{cases}$$

STRIPS Planning: Semantics

Definition (STRIPS State Space). Let $\Pi = (P, A, c, I, G)$ be a STRIPS planning task. The *state space* of Π is the labeled transition system $\Theta_\Pi = (S, L, c, T, I, S^G)$ where:

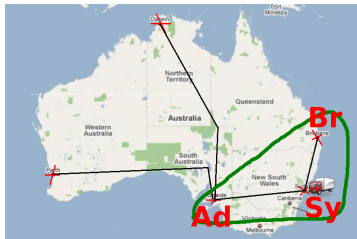
- The *states* (also *world states*) $S = 2^P$ are the subsets of P .
- The labels $L = A$ are Π 's actions; the cost function c is that of Π .
- The transitions are $T = \{s \xrightarrow{a} s' \mid a \in A[s], s' = s[a]\}$, where
 $A[s] := \{a \in A \mid pre_a \subseteq s\}$ are the actions *applicable* in s ; for $a \in A[s]$,
 $s[a] := (s \cup add_a) \setminus del_a$; for $a \notin A[s]$, $s[a]$ is *undefined*, $s[a] := \perp$.
- The initial state I is identical to that of Π .
- The goal states $S^G = \{s \in S \mid G \subseteq s\}$ are those that satisfy Π 's goal.

An (optimal) *plan* for $s \in S$ is an (optimal) solution for s in Θ_Π . A solution for I is called a *plan for Π* . Π is *solvable* if a plan for Π exists.

For $\vec{a} = \langle a_1, \dots, a_n \rangle$, $s[\vec{a}] := \begin{cases} s & n = 0 \\ s[\langle a_1, \dots, a_{n-1} \rangle][a_n] & n > 0 \end{cases}$

→ Is Θ_Π *deterministic*? Yes: the successor state s' in $s \xrightarrow{a} s'$ is uniquely determined by s and a , through $s' = s[a]$.

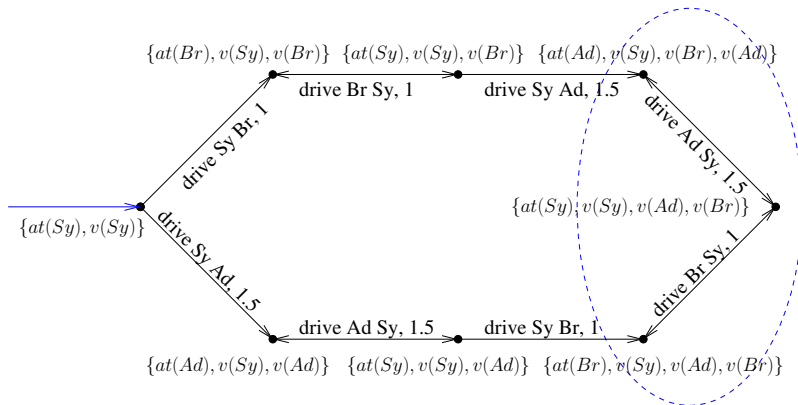
STRIPS Encoding of Simplified “TSP”



- **Propositions** P : $\{at(x), visited(x) \mid x \in \{Sydney, Adelaide, Brisbane\}\}$.
- **Initial state** I : $\{at(Sydney), visited(Sydney)\}$.
- **Goal** G : $\{visited(x) \mid x \in \{Sydney, Adelaide, Brisbane\}\}$. (Note: no “ $at(Sydney)$ ”.)
- **Actions** $a \in A$: $drive(x, y)$ where x, y have a road.
 - Precondition** pre_a : $\{at(x)\}$.
 - Add list** add_a : $\{at(y), visited(y)\}$.
 - Delete list** del_a : $\{at(x)\}$.
- **Cost function** c :

$$c(drive(x, y)) = \begin{cases} 1 & \{x, y\} = \{Sydney, Brisbane\} \\ 1.5 & \{x, y\} = \{Sydney, Adelaide\} \end{cases}$$

STRIPS Encoding of Simplified “TSP”: State Space



→ Exactly one optimal plan: drive Sy Br, drive Br Sy, drive Sy Ad.

→ **Is this actually the state space?** No, only the reachable part. E.g., Θ_{Π} also includes the states $\{v(Sy)\}$ and $\{at(Sy), at(Br)\}$.

Questionnaire



- **Propositions** P :
 $\{at(x), visited(x) \mid x \in \{Sydney, Adelaide, Brisbane, Perth, Darwin\}\}.$
- **Initial state** I : $\{at(Sydney), visited(Sydney)\}.$

How many states are there in the “TSP in Australia” task?

→: $2^{10} = 1024$. But only a small portion of them are reachable (less than $5 \cdot 2^4 = 80$)!

FDR Planning: Syntax

Definition (FDR Planning Task). A *finite-domain representation planning task*, short *FDR planning task*, is a 5-tuple $\Pi = (V, A, c, I, G)$ where:

- V is a finite set of *state variables*, each $v \in V$ with a finite domain D_v . We refer to (partial) functions on V , mapping each $v \in V$ into a member of D_v , as (partial) *variable assignments*.
- A is a finite set of *actions*; each $a \in A$ is a pair (pre_a, eff_a) of *partial variable assignments* referred to as the action's *precondition* and *effects*.
- $c : A \mapsto \mathbb{R}_0^+$ is the *cost function*.
- I is a complete variable assignment called the *initial state*.
- G is a partial variable assignment called the *goal*.

We say that Π has *unit costs* if, for all $a \in A$, $c(a) = 1$.

→ In FDR, a (partial) variable assignment represents a state in I , a condition in pre_a and G , and an effect instruction in eff_a .

Notation: Pairs (v, d) are *facts*, also written $v = d$. We identify partial variable assignments p with fact sets. We write $V[p] := \{v \in V \mid p(v) \text{ is defined}\}$.

FDR Encoding of “TSP”



- **Variables** V : $at : \{Sydney, Adelaide, Brisbane, Perth, Darwin\}$; $visited(x) : \{T, F\}$ for $x \in \{Sydney, Adelaide, Brisbane, Perth, Darwin\}$.
- **Initial state** I : $at = Sydney, visited(Sydney) = T, visited(x) = F$ for $x \neq Sydney$.
- **Goal** G : $at = Sydney, visited(x) = T$ for all x .
- **Actions** $a \in A$: $drive(x, y)$ where x, y have a road.
 Precondition pre_a : $at = x$.
 Effect eff_a : $at = y, visited(y) = T$.

- **Cost function** c :

$$c(drive(x, y)) = \begin{cases} 1 & \{x, y\} = \{Sydney, Brisbane\} \\ 1.5 & \{x, y\} = \{Sydney, Adelaide\} \\ 3.5 & \{x, y\} = \{Adelaide, Perth\} \\ 4 & \{x, y\} = \{Adelaide, Darwin\} \end{cases}$$

FDR Planning: Semantics

Definition (FDR State Space). Let $\Pi = (V, A, c, I, G)$ be an FDR planning task. The *state space* of Π is the labeled transition system

$\Theta_\Pi = (S, L, c, T, I, S^G)$ where:

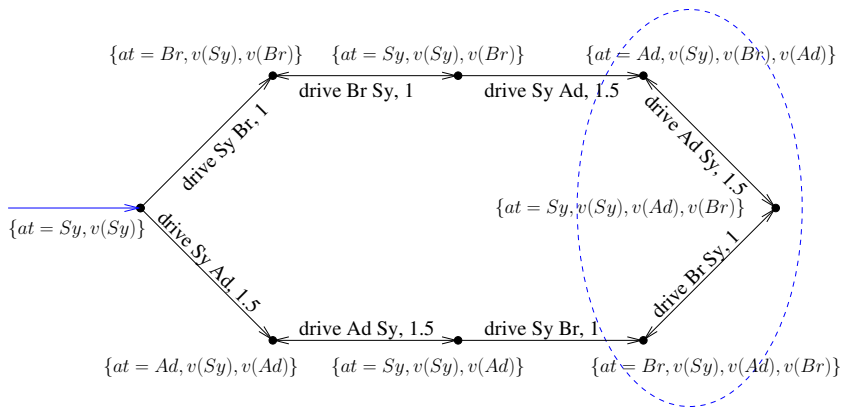
- The *states* (also *world states*) S are the complete variable assignments.
- The labels $L = A$ are Π 's actions; the cost function c is that of Π .
- The transitions are $T = \{s \xrightarrow{a} s' \mid a \in A[s], s' = s[a]\}$, where
 $A[s] := \{a \in A \mid pre_a \subseteq s\}$ are the actions *applicable* in s ; for $a \notin A[s]$,
 $s[a] := \perp$; for $a \in A[s]$, $s[a](v) := \begin{cases} eff_a(v) & v \in V[eff_a] \\ s(v) & v \notin V[eff_a] \end{cases}$
- The initial state I is identical to that of Π .
- The goal states $S^G = \{s \in S \mid G \subseteq s\}$ are those that satisfy Π 's goal.

→ In $s[a]$, instead of “adding/deleting” facts, we overwrite the previous variable values by eff_a .

→ Plan, optimal plan, $s[\vec{a}]$ for action sequence \vec{a} : as before (slide 19).

FDR Encoding of Simplified “TSP”: State Space

(using “ $v(x)$ ” as shorthand for $visited(x) = T$)



→ This is only the reachable part of the state space: E.g., Θ_{Π} also includes the state $\{at = Sy, v(Br)\}$. (But neither $\{v(Sy)\}$ nor $\{at = Sy, at = Br\}$, compare slide 21.)

Questionnaire

Question!

How many STRIPS state variables are needed to encode the problem of finding a path in a graph with n vertices?

(A): 1

(B): n

(C): $\lceil \log_2 n \rceil$

(D): $2 * \lceil \log_2 n \rceil$

→ (D): We need to encode our current position in the graph. This can be done with n propositions of the form " $at(p)$ ", but it can be done more compactly by: numbering the positions $ID(p)$; representing $ID(p)$ in the binary system using $\lceil \log_2 n \rceil$ bits bit_i ; and representing each bit_i with two STRIPS facts $True(bit_i)$ and $False(bit_i)$.

Question!

How many FDR state variables are needed for this?

(A): 1

(B): n

(C): $\lceil \log_2 n \rceil$

(D): $2 * \lceil \log_2 n \rceil$

→ (A): We need 1 variable with n values, encoding our current position in the graph.

STRIPS vs. FDR in Practice

How do people use FDR?

- Our surface language is PDDL, which corresponds to STRIPS.
- Most implemented planning tools are based on **Fast Downward (FD)** [Helmert (2009)], which reads PDDL input, then internally uses a “clever” **STRIPS-2-FDR translation** (see next).
- That translation involves a **PSPACE**-complete sub-problem.

Why??? Practical Efficiency!

- **Regression**: FDR avoids myriads of unreachable states. → **Chapter 6**
- **Causal Graphs**: Capture variable dependencies; have a much clearer structure for clever FDR (e.g., acyclic vs. cyclic). → **Chapter 5**
- **Complexity Analysis**: Better with clearer causal graph. → **Chapter 5**
- **Construction of Heuristic Functions**: Better with multiple-valued variables and clearer causal graph. → **Chapters 10 and 12**
- **Modeling**: Anyway, FDR is more natural! (It's just one truck, after all.)

Why does anybody use STRIPS? It's a legacy system.

→ We should be modeling in FDR. For historical reasons, we aren't.

STRIPS vs. FDR Conversions

Conversions:

- ❶ **FDR-2-STRIPS**: For each variable v with domain $\{d_1, \dots, d_k\}$, make k STRIPS facts " $v = d_1$ ", \dots , " $v = d_k$ ".
- ❷ **STRIPS-2-FDR**: Naïve vs. clever variants, see slides 34 – 37.

What role does all this play here?

- Both STRIPS and FDR are used in practice, cf. slide 30. The **programming exercises** are in FD, hence FDR.
- Some techniques in the remainder of the course are easier to introduce in STRIPS, some are easier in FDR, so we will keep both around.
- Specific **relevance of (I)**: If the course introduces a technique A in STRIPS, then A in FDR (and hence your FD code!) is equivalent to "convert-FDR-2-STRIPS-then-do- A ".
- Specific **relevance of (II)**: So you get an understanding of how FD processes the PDDL/STRIPS input to FDR.

FDR-2-STRIPS: Details

Definition (FDR-2-STRIPS). Let $\Pi = (V, A, c, I, G)$ be an FDR planning task. The *STRIPS conversion* of Π is the STRIPS task

$\Pi^{\text{STR}} = (P_V, A^{\text{STR}}, c, I, G)$ where:

- $P_V = \{v = d \mid v \in V, d \in D_v\}$ is the set of (STRIPS) *facts*.
- $A^{\text{STR}} = \{a^{\text{STR}} \mid a \in A\}$ where $\text{pre}_{a^{\text{STR}}} = \text{pre}_a$, $\text{add}_{a^{\text{STR}}} = \text{eff}_a$, and

$$\text{del}_{a^{\text{STR}}} = \bigcup_{(v=d) \in \text{eff}_a} \begin{cases} \{v = \text{pre}_a(v)\} & \text{if } \text{pre}_a(v) \text{ is defined} \\ \{v = d' \mid d' \in D_v \setminus \{d\}\} & \text{otherwise} \end{cases}$$
- The cost function c is defined by $c(a^{\text{STR}}) := c(a)$ for all $a^{\text{STR}} \in A^{\text{STR}}$.
- I and G are identical to those of Π .

→ The adds establish the new variable values of eff_a ; the deletes make sure to erase the previous values of those variables.

→ Take-home message: **FDR variable/value pairs \approx STRIPS facts!**

Proposition. Let $\Pi = (V, A, c, I, G)$ be an FDR planning task, and let Π^{STR} be its STRIPS conversion. Then Θ_Π is isomorphic to the sub-system of $\Theta_{\Pi^{\text{STR}}}$ induced by those $s \subseteq P_V$ where, for each $v \in V$, s contains exactly one fact of the form $v = d$. All other states in $\Theta_{\Pi^{\text{STR}}}$ are unreachable.

FDR-2-STRIPS: Simplified “TSP”



- **FDR V :** $at : \{Sydney, Adelaide, Brisbane\}; visited(x) : \{T, F\}$ for $x \in \{Sydney, Adelaide, Brisbane\}$.
- **STRIPS P :** $at(x), visited(x, T), visited(x, F)$ for $x \in \{Sydney, Adelaide, Brisbane\}$.
- **FDR $dr(x, y)$:** $pre = \{at = x\}, eff = \{at = y, v(y) = T\}$.
- **STRIPS $dr(x, y)$:**
 $pre = \{at(x)\}, add = \{at(y), v(y, T)\}, del = \{at(x), v(y, F)\}$.

STRIPS-2-FDR: Naïve Translation

Definition (STRIPS-2-FDR). Let $\Pi = (P, A, c, I, G)$ be a STRIPS planning task. The *FDR conversion* of Π is the FDR task

$\Pi^{\text{FDR}} = (V_P, A^{\text{FDR}}, c, I^{\text{FDR}}, G^{\text{FDR}})$ where:

- $V_P = \{v_p \mid p \in P\}$ is the set of variables, all Boolean.
- $A^{\text{FDR}} = \{a^{\text{FDR}} \mid a \in A\}$ where $\text{pre}_{a^{\text{FDR}}} = \{v_p = T \mid p \in \text{pre}_a\}$ and $\text{eff}_{a^{\text{FDR}}} = \{v_p = T \mid p \in \text{add}_a\} \cup \{v_p = F \mid p \in \text{del}_a\}$.
- The cost function c is defined by $c(a^{\text{FDR}}) := c(a)$ for all $a^{\text{FDR}} \in A^{\text{STR}}$.
- $I = \{v_p = T \mid p \in I\}$; and $G = \{v_p = T \mid p \in G\}$.

→ All variables here have two possible values only, so this does not benefit at all from the added expressivity of FDR. Hence the designation “naïve”.

Proposition. Let $\Pi = (P, A, c, I, G)$ be a STRIPS planning task, and let Π^{FDR} be its STRIPS conversion. Then Θ_Π is isomorphic to $\Theta_{\Pi^{\text{STR}}}$.

STRIPS-2-FDR, Naïve: Simplified “TSP”



- **STRIPS P :** $at(x), visited(x)$ for $x \in \{Sydney, Adelaide, Brisbane\}$.
- **FDR V :** $at(x), visited(x) : \{T, F\}$ for $x \in \{Sydney, Adelaide, Brisbane\}$.
- **STRIPS $dr(x, y)$:** $pre = \{at(x)\}$, $add = \{at(y), v(y)\}$, $del = \{at(x)\}$
- **FDR $dr(x, y)$:** $pre = \{at(x) = T\}$,
 $eff = \{at(y) = T, v(y) = T, at(x) = F\}$.

STRIPS-2-FDR: Clever Translation

How to be clever?

- Find sets $\{p_1, \dots, p_k\}$ of STRIPS facts so that every reachable state s makes exactly one p_i true.
→ Deciding whether this holds, for a given $\{p_1, \dots, p_k\}$, is **PSPACE**-complete (cf. slide 30). But one can design fast algorithms finding *some* such sets [Helmert (2009)].
- For each set $\{p_1, \dots, p_k\}$ found, make *one* FDR variable v with domain $\{d_1, \dots, d_k\}$.
- This is implemented in the pre-processor of [Fast Downward](#).

STRIPS-2-FDR Naïve vs. Clever: Simplified “TSP”



- **STRIPS** P : $at(x), visited(x)$ for $x \in \{Sydney, Adelaide, Brisbane\}$.
- **Naïve** V : $at(x), visited(x) : \{T, F\}$ for $x \in \{Sydney, Adelaide, Brisbane\}$.
- **Clever** V : $at : \{Sydney, Adelaide, Brisbane\};$
 $visited(x) : \{T, F\}$ for $x \in \{Sydney, Adelaide, Brisbane\}$.

→ The naïve version is merely STRIPS in disguise. The clever version is more natural, and is explicit about the “truck position”.

Action Description Language (ADL)

Framework Definition: [Pednault (1989); Hoffmann and Nebel (2001)].

Problem: Like STRIPS but with **PL1 formulas** in pre_a and G , and with **conditional effects** that execute only if their individual effect condition holds.

Plan: Sequence of actions. (Yes, this is still “classical planning”.)

Example: If your action a opens the doors of an elevator, then each passenger gets out iff their individual condition (“Is this my destination floor?”) holds. If you want to satisfy complex constraints (“Group A should never meet group B in the elevator”) then pre_a gets nasty. (See the PDDL file [here](#).)

Compilation: PL1 formulas: Ground them (the universe is finite) and transform to DNF [Gazen and Knoblock (1997); Koehler and Hoffmann (2000)].

Conditional effects: Either enumerate all combinations of effects, or introduce artificial facts/actions enforcing an “effect evaluation phase” [Nebel (2000)].

State of the art: Get rid of PL1 formulas but keep the conditional effects [Hoffmann and Nebel (2001)].

Numeric and Temporal Planning



Numeric Planning: [Fox and Long (2003)]

$pre_a : fuelSupply \geq distance(x, y) * fuelConsumption$

$eff_a : fuelSupply := fuelSupply - distance(x, y) * fuelConsumption$

Compilation: Nothing known.

Temporal Planning: [Fox and Long (2003)]

$duration_a : distance(x, y) / speed$

$eff_a : at\ Start \neg at(x), at\ End\ at(y).$

Compilation: Ignore durations during search, schedule plan as a post-process [Edelkamp (2003)]. **Competitive with state of the art!**

Soft Goals and Trajectory Constraints



Soft Goals: [Gerevini *et al.* (2009)]

“I don’t absolutely have to visit Darwin, but if I do, I get a certain amount R of reward.”

Compilation: Artificial actions that allow to forgo each weak goal, at cost R ; minimize cost [Keyder and Geffner (2009)]. **State of the art!**

Trajectory Constraints: [Gerevini *et al.* (2009)]

“I must visit Perth before I visit Darwin.”

Compilation: Artificial preconditions/effects, e.g. *visited(Perth)* into precondition of driving to Darwin [Edelkamp (2006)]. **State of the art!**

Conformant Planning

Framework Definition: [Smith and Weld (1998); Bonet and Givan (2006)].

Problem: There are **many possible initial states** (represented as a formula), and each action may have **several possible effects**. We have **no observability** during plan execution.

Plan: Sequence of actions that **achieves the goal regardless which initial state and action effects occur**.

Example: You're in a dark cave but don't know where exactly. The plan is to walk to the right until you reach a wall and can locate yourself (thanks to noticing that the action "walk to the right" does not work anymore). Then navigate to your goal by counting your steps.

Compilation: Artificial "what-if" facts, like "If I was at A initially, then I am now at B" [Palacios and Geffner (2009)]. **State of the art!**

Contingent Planning

Framework Definition: e.g., [Hoffmann and Brafman (2005)].

Problem: There are many possible initial states (represented as a formula), and each action may have several possible effects. We have **partial observability** during plan execution.

Plan: **Tree of actions** that achieves the goal in each of its leaves. (“Plan ahead for all possible contingencies, i.e., situation aspects not known at planning time.”)

Example: Solving the Wumpus world: You walk some steps, then use sensing (for breeze and stench), and continue depending on the outcome.

Compilation: Sample initial states, classical planning with artificial facts encoding knowledge yields a plan tree for those; in case a problem is detected during execution, re-plan with the new state of knowledge [Shani and Brafman (2011)]. **Competitive with state of the art!**

Probabilistic Planning

Framework Definition: e.g., [Younes *et al.* (2005)].

Problem: Each action specifies a **probability distribution over its possible effects**. We have **full observability** during plan execution. (**Markov Decision Process (MDP)** framework.)

Plan: **Policy** that maps states to actions in a way that maximizes the expected reward.

Example: Controlling a robot: If navigation comes with an imprecision (which it usually does), then the outcome of a “move” operation is uncertain.

Compilation: Make classical problem that acts as if you could *choose* the outcomes; find a plan, and execute; if the plan fails, then re-plan from the current state [Yoon *et al.* (2007)]. **State of the art for problems where “reactive behavior” is suitable** (things may go wrong, but if they do, they can be easily repaired).

Summary

- **Transition systems** are a kind of directed graph (typically huge) that encode how the state of the world can change.
- **Planning tasks** are compact representations for transition systems, based on state variables; they are the input for **planning systems**.
- In **satisficing planning**, we must find a solution to planning tasks (or show that no solution exists). In **optimal planning**, we must additionally guarantee that generated solutions are the cheapest possible.
- **Classical planning** makes strong simplifying assumptions, but is very successful in practice and can be used by **compilation** to tackle more expressive planning problems.
- In **STRIPS**, state variables are Boolean; in **FDR**, they may have arbitrary finite domains. The two formalisms can be compiled into each other. FDR is preferable, but current planning technology is based on STRIPS for historical reasons.
→ **PDDL**, see **Next Chapter**.

Remarks

Regarding the name “FDR”:

- FDR is not consistently named in the literature.
- It is often referred to as **SAS⁺** because that's what some complexity guys called it, in the first papers considering a formalism equivalent to our FDR [e.g., Bäckström and Nebel (1995)].
- [Helmert (2006)] called it **multi-valued planning tasks (MPT)** which can still be seen in some papers.
- [Helmert (2009)] finally called it FDR.

Reading

- *Concise Finite-Domain Representations for PDDL Planning Tasks* [Helmert (2009)].

Available at:

[http://www.informatik.uni-freiburg.de/~ki/papers/
helmert-aij2009.pdf](http://www.informatik.uni-freiburg.de/~ki/papers/helmert-aij2009.pdf)

Content: Describes in detail the “clever” STRIPS-2-FDR conversion implemented in Fast Downward. The sets $\{p_1, \dots, p_k\}$ of STRIPS facts, of which exactly one is true in every reachable state, are found by automatic **invariance analysis**. Is in wide-spread use, and a basic familiarity with it is relevant for anybody working in planning.

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