

# Novel Is Not Always Better: On the Relation between Novelty and Dominance Pruning

Joschka Groß, Álvaro Torralba, Maximilian Fickert



UNIVERSITÄT  
DES  
SAARLANDES



**CISPA**  
HELMHOLTZ CENTER FOR  
INFORMATION SECURITY

# Classical Planning

**Definition.** A *planning task* is a 4-tuple  $\Pi = (V, A, I, G)$  where:

- $V$  is a set of *state variables*, each  $v \in V$  with a finite *domain*  $D_v$ .
- $A$  is a set of *actions*; each  $a \in A$  is a triple  $(pre_a, eff_a, c_a)$ , of *precondition* and *effect* (partial assignments), and the action's *cost*  $c_a \in \mathbb{R}_0^+$ .
- *Initial state*  $I$  (complete assignment), *goal*  $G$  (partial assignment).

→ **Solution ("Plan"):** Action sequence mapping  $I$  into  $s$  s.t.  $s \models G$ .

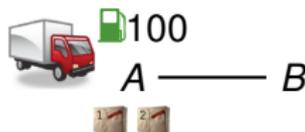
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**Running Example:**



- $V = \{t, p_1, p_2, f\}$   
with  $D_t = \{A, B\}$  and  $D_{p_i} = \{t, A, B\}$ ,  $D_f = \{100, 99, 98, \dots, 0\}$ .
- $A = \{load(p_i, x), unload(p_i, x), drive(x, x')\}$

## What this is about?

**Novelty** (Lipovetzky and Geffner, 2012) (Lipovetzky and Geffner, 2017) (Katz, Lipovetzky, Moshkovich and Tuisov 2017) (Fickert 2018)

A (pruning) technique which has **greatly improved the state of the art in satisficing planning**

**Dominance** (Torralba and Hoffmann, 2015), (Torralba, 2017), (Torralba, 2018):

A safe pruning technique for **cost-optimal planning**

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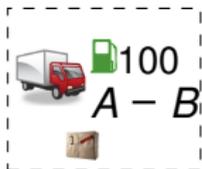
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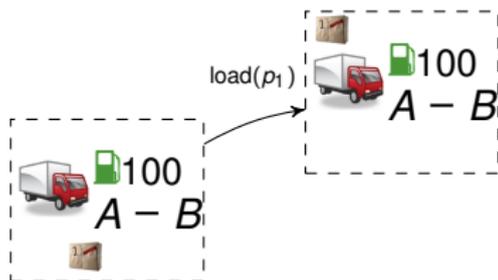
But, why is novelty so good?

# Example IW(1)



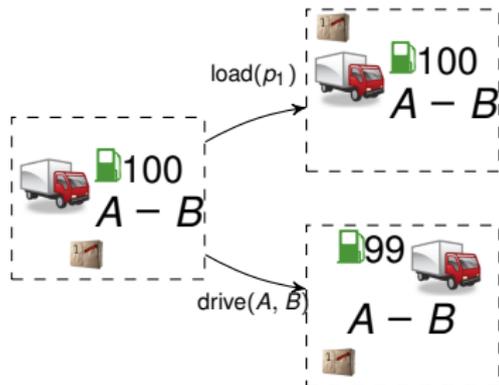
A	B	A	B	T	100	99	98	97
X		X			X			

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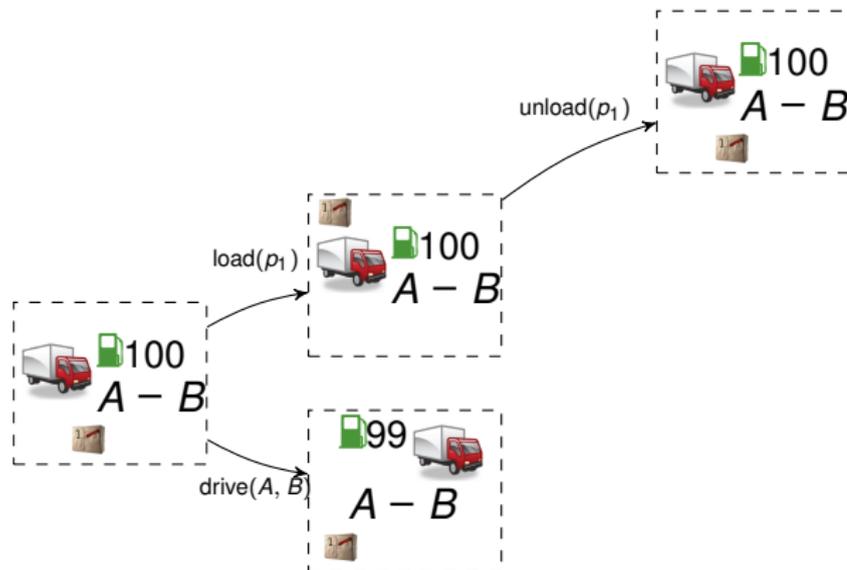
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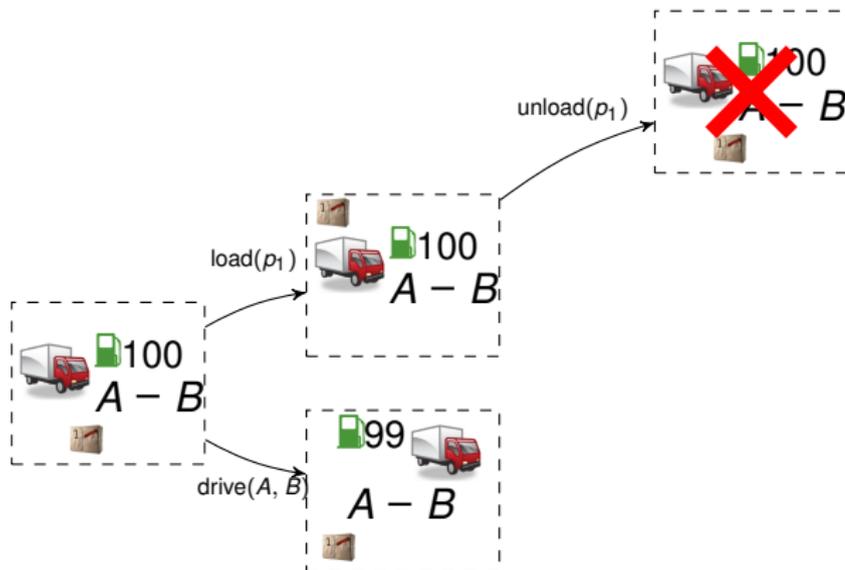
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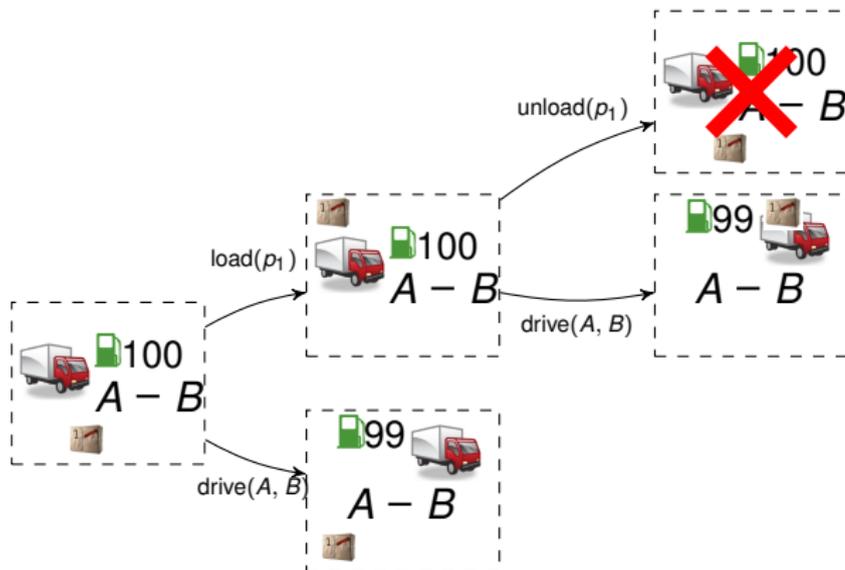
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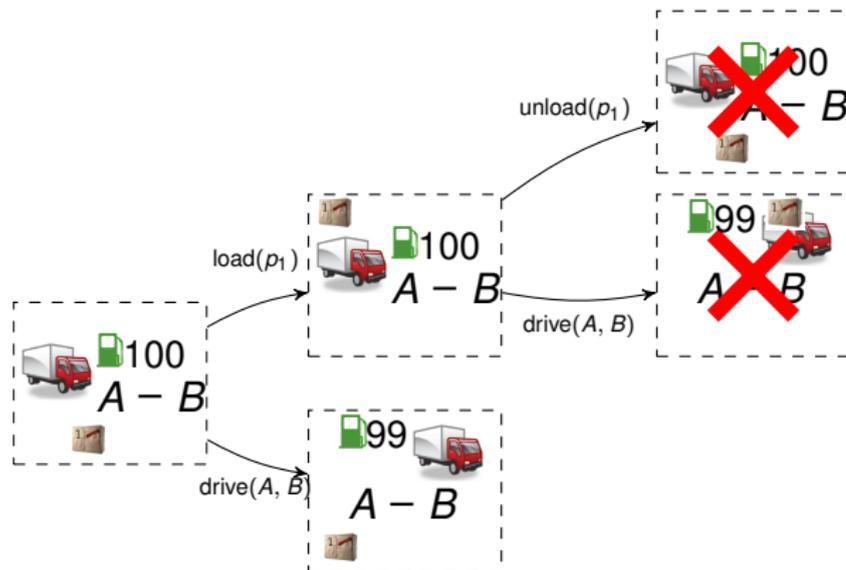
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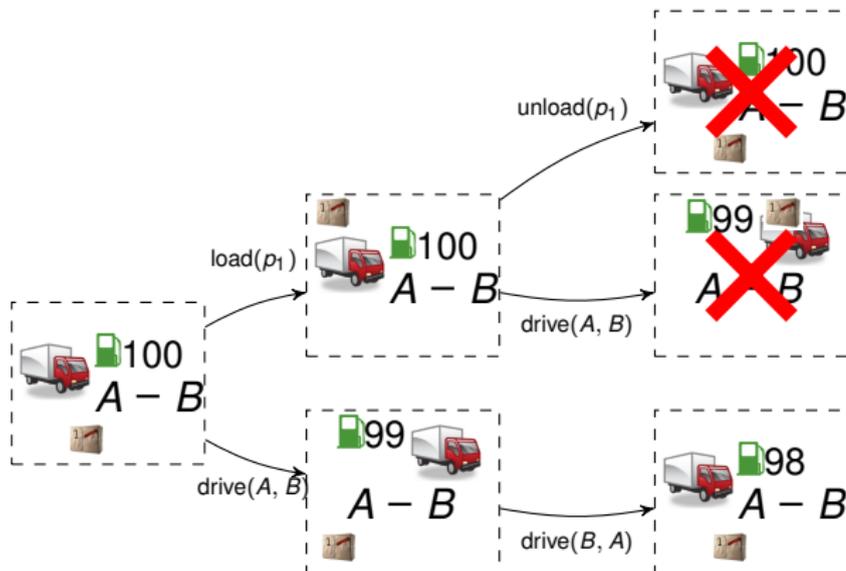
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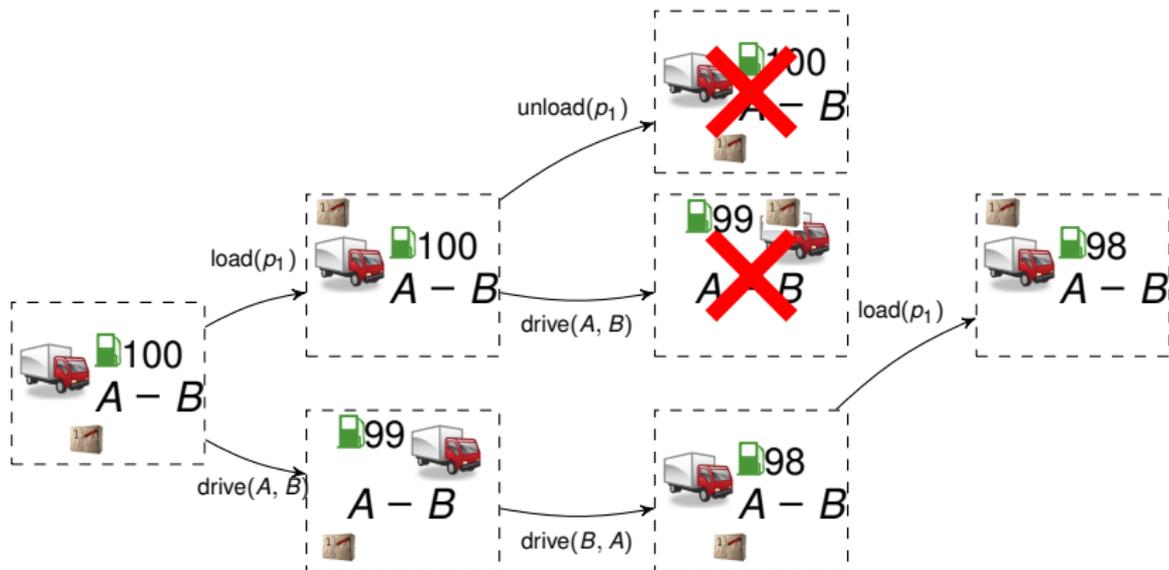
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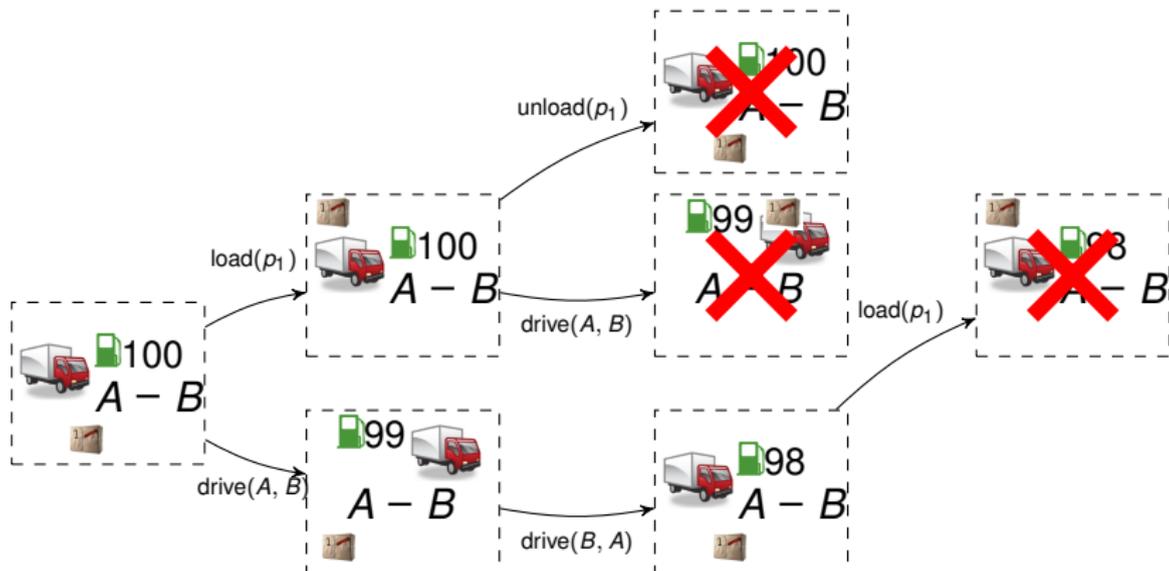
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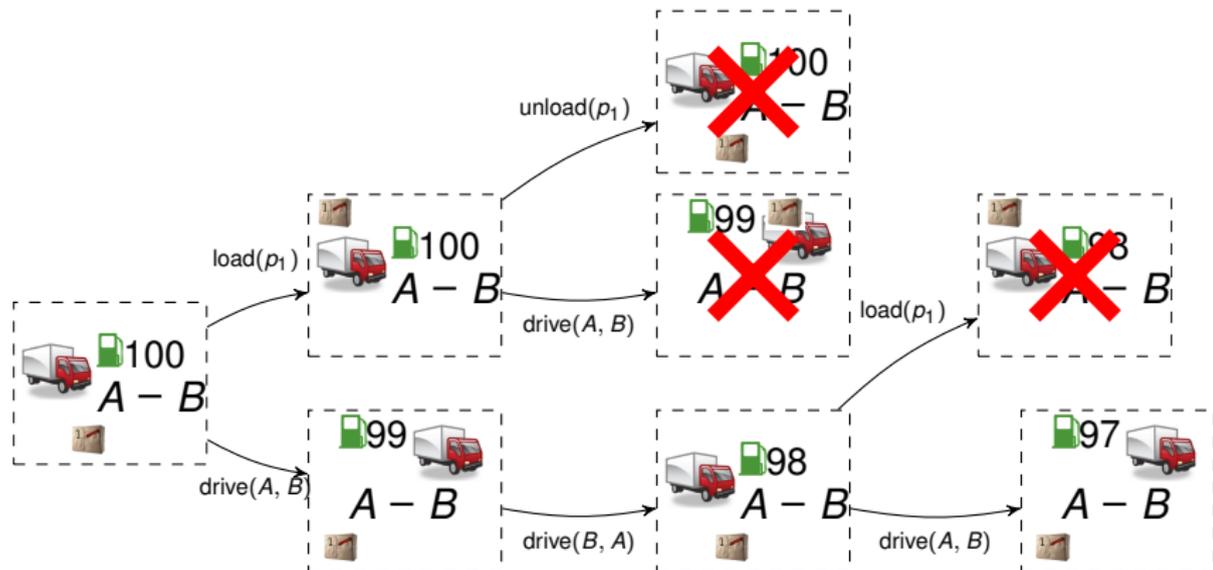
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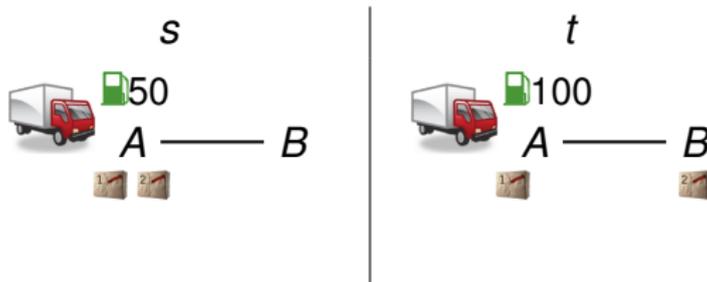
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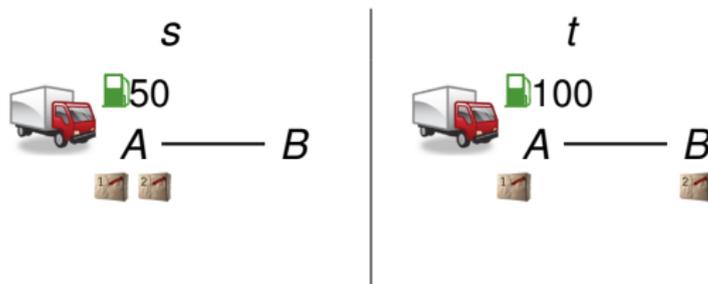
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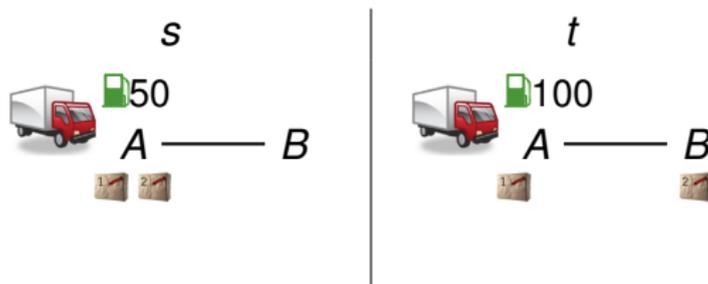


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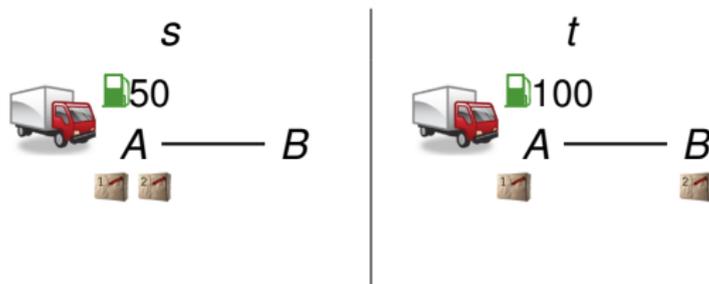


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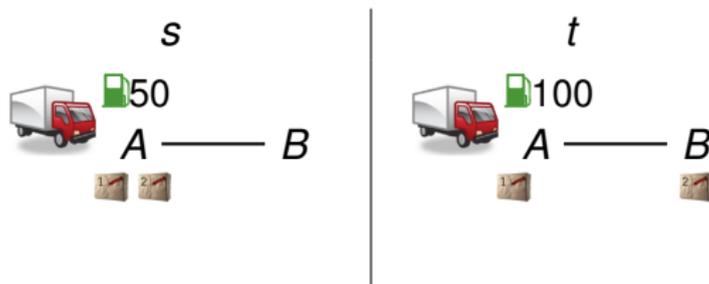
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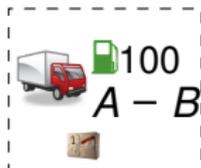
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$$\text{package 1} : A \preceq B \quad \text{package 2} : A \preceq B \quad \text{fuel} : 0 \preceq 1 \preceq 2 \preceq 3 \dots$$

(no matter the position of other packages or trucks)

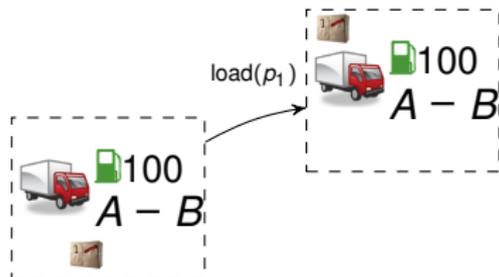
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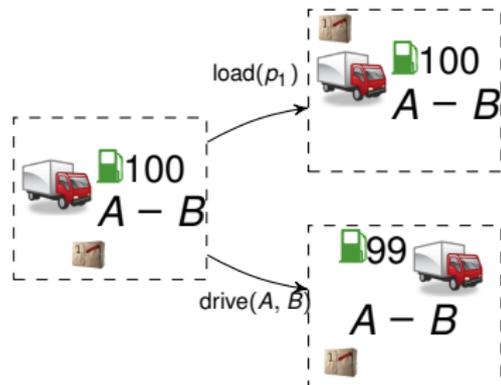
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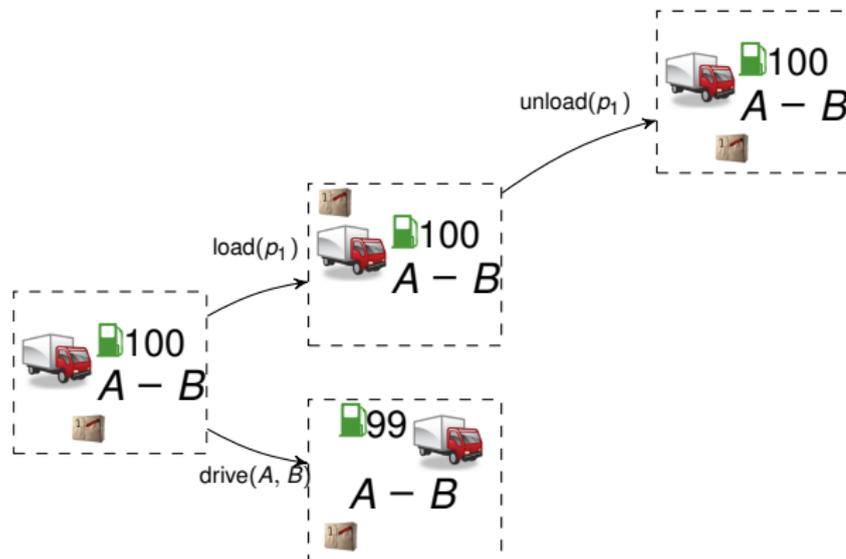
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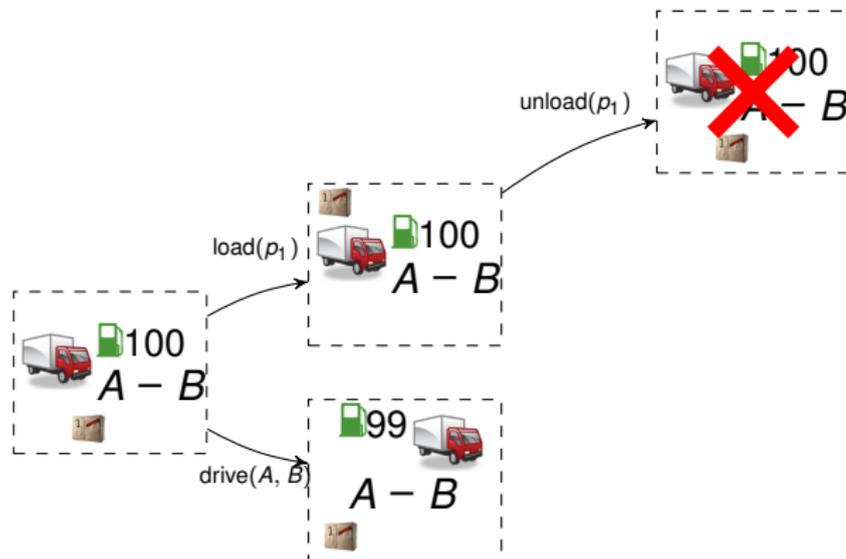
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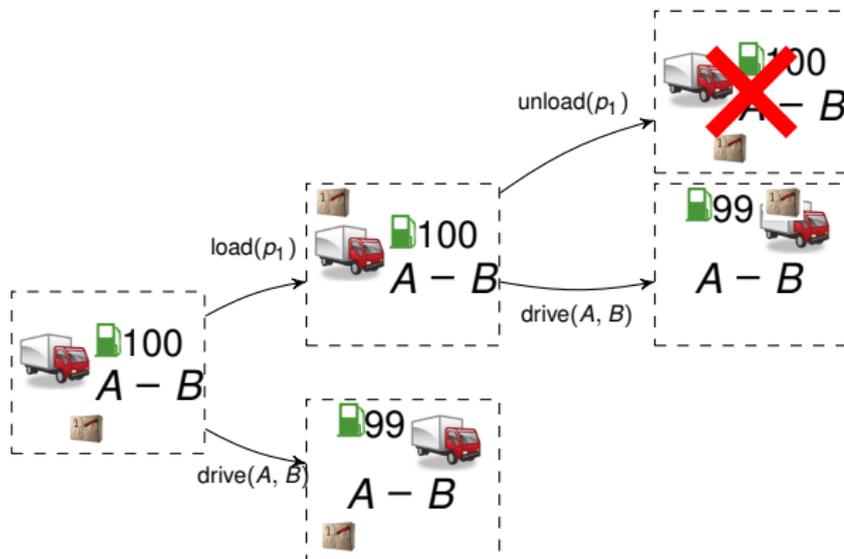
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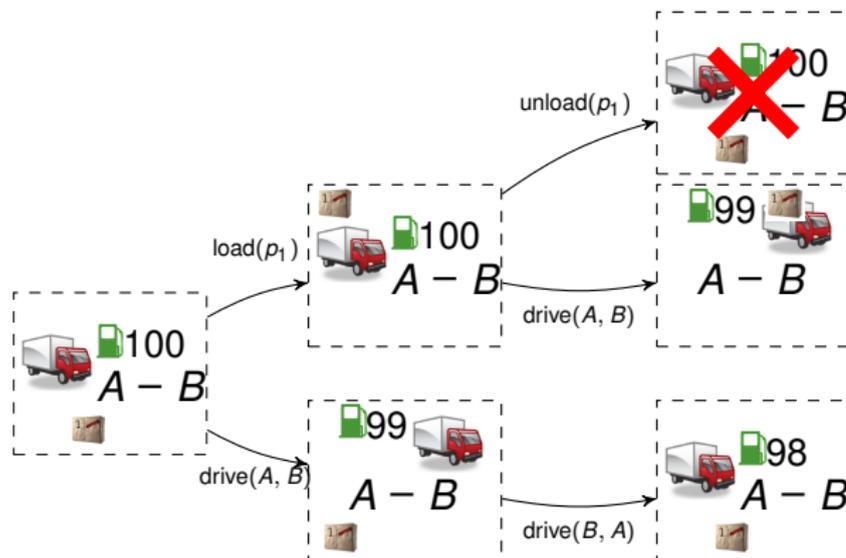
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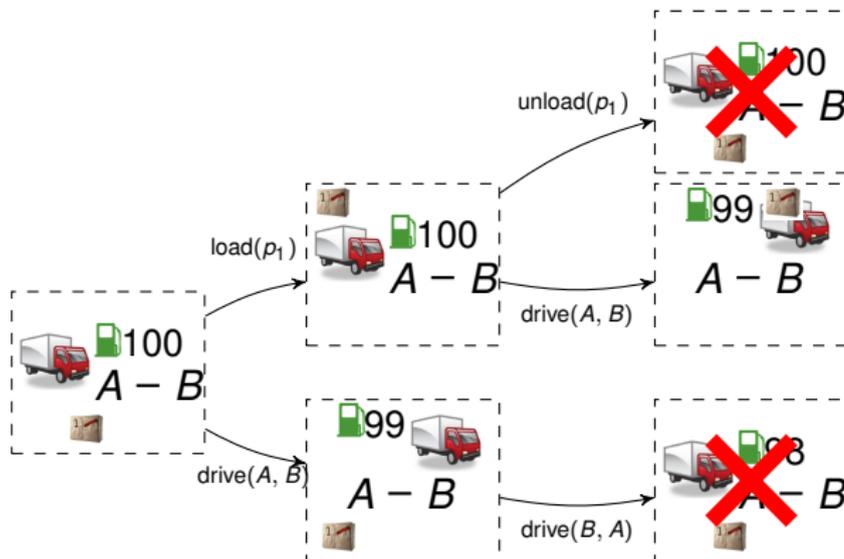
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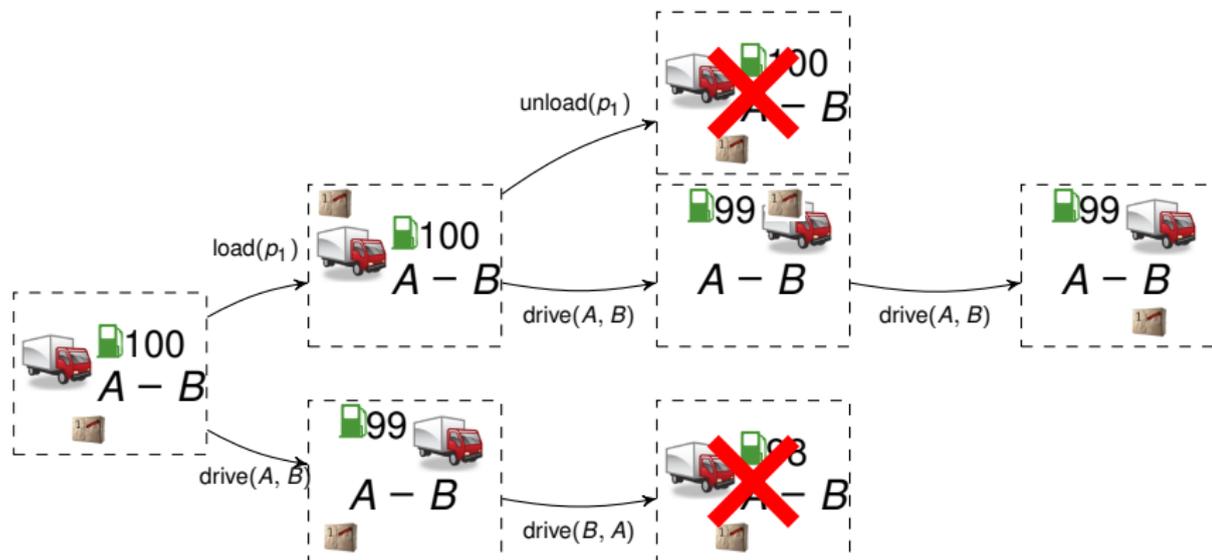
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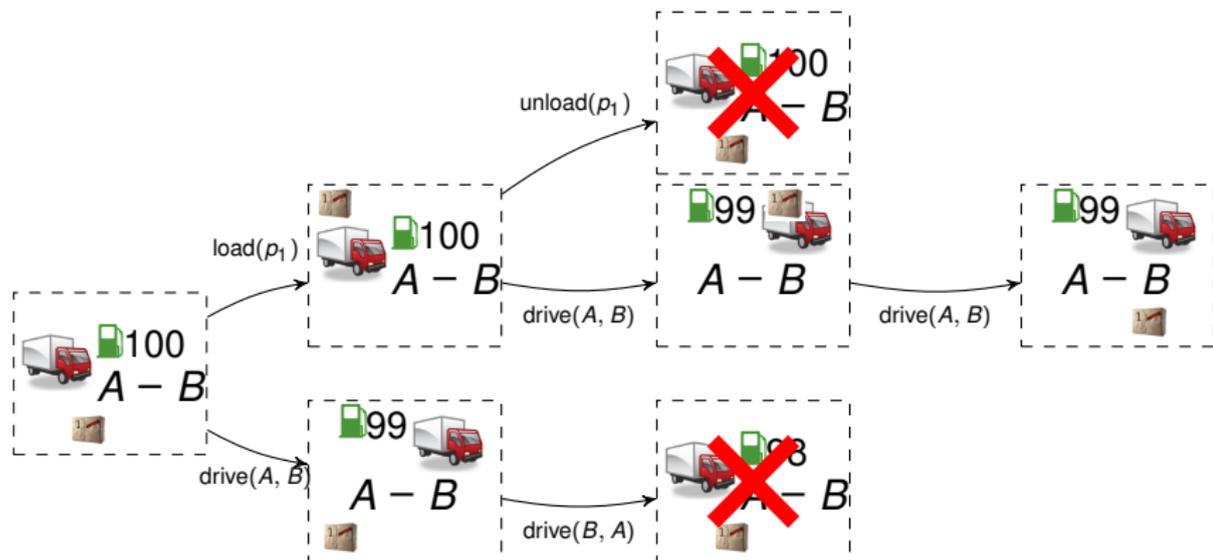
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→ Dominance pruning preserves at least an optimal solution.

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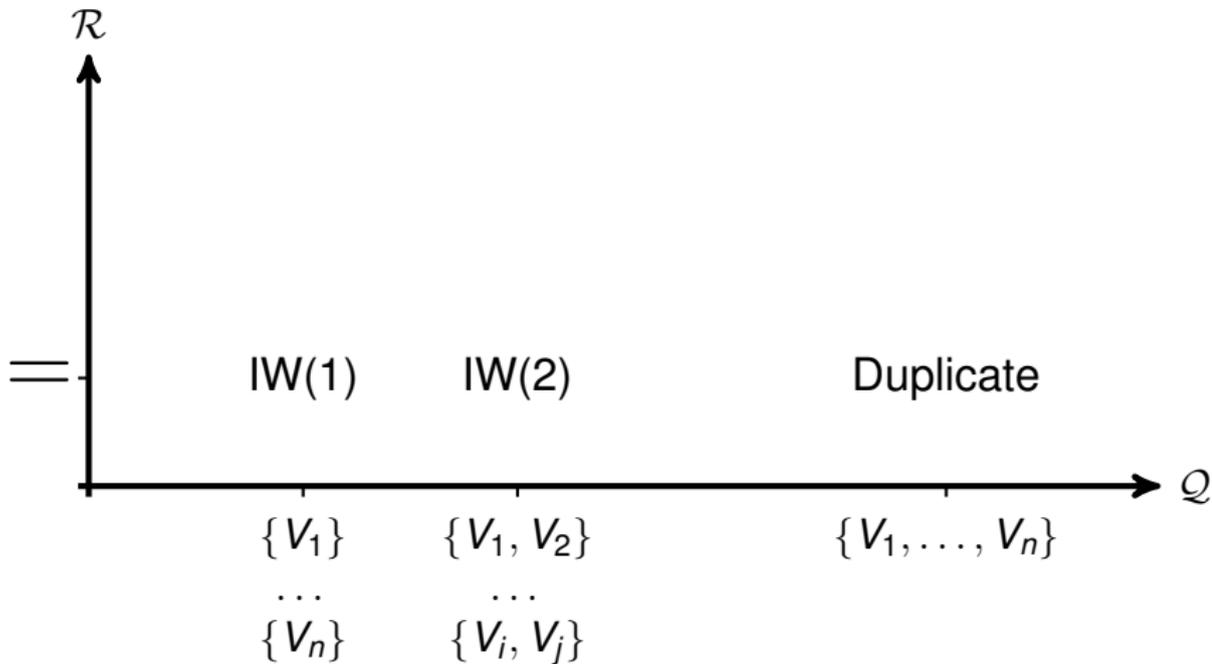
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Let  $\mathcal{R} = \{\preceq_1, \dots, \preceq_k\}$  be a set of relations on  $P$ .

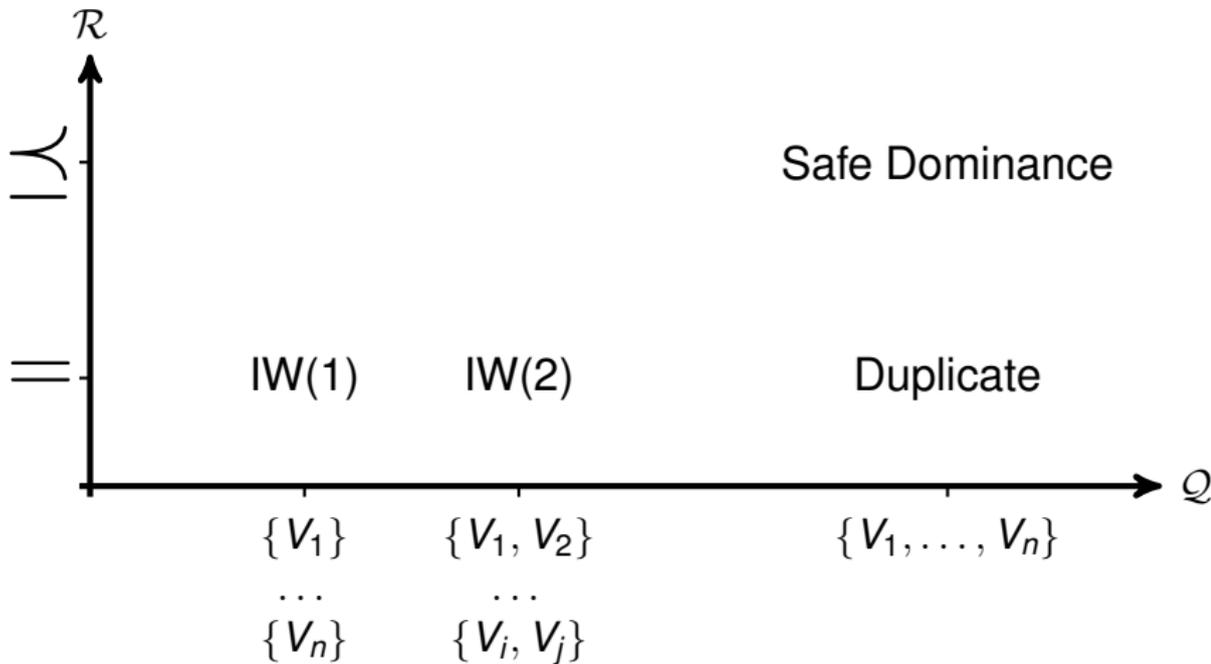
Let  $\mathcal{Q}$  be a set of subsets of  $V$ .

$$\forall Q \in \mathcal{Q} : \exists t \in \mathcal{T} : \forall v \in Q : s[v] \preceq t[v]$$

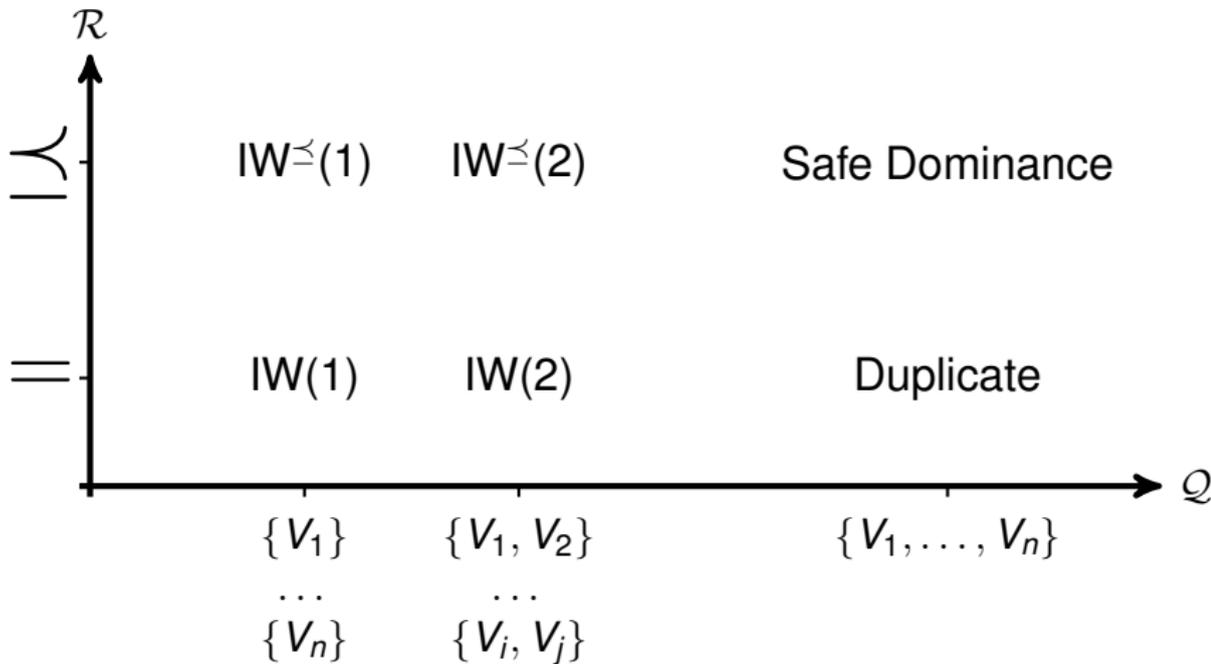
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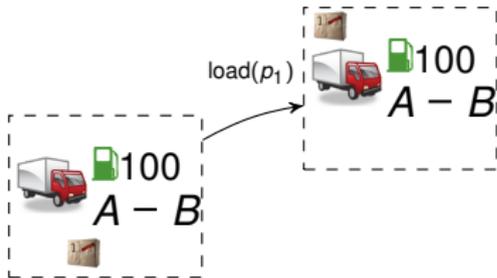
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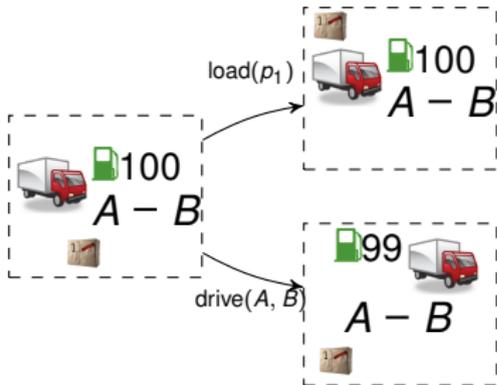
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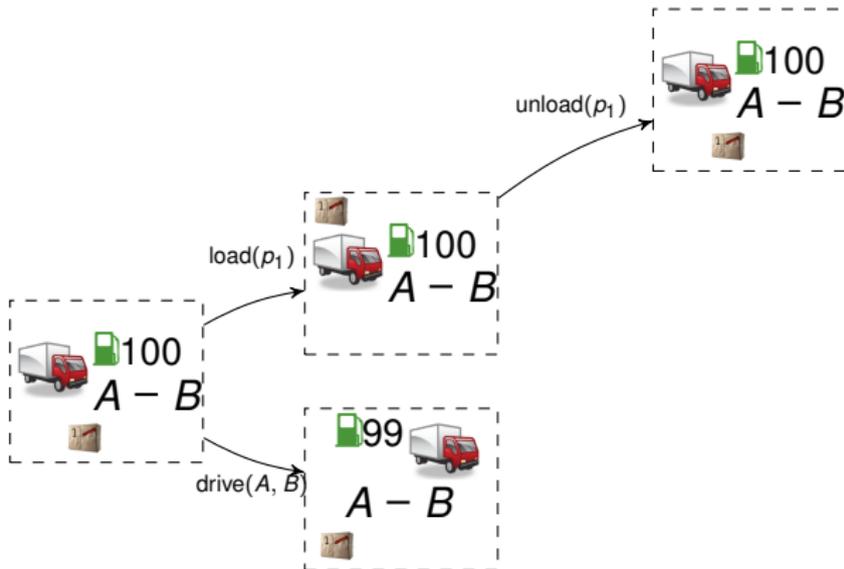


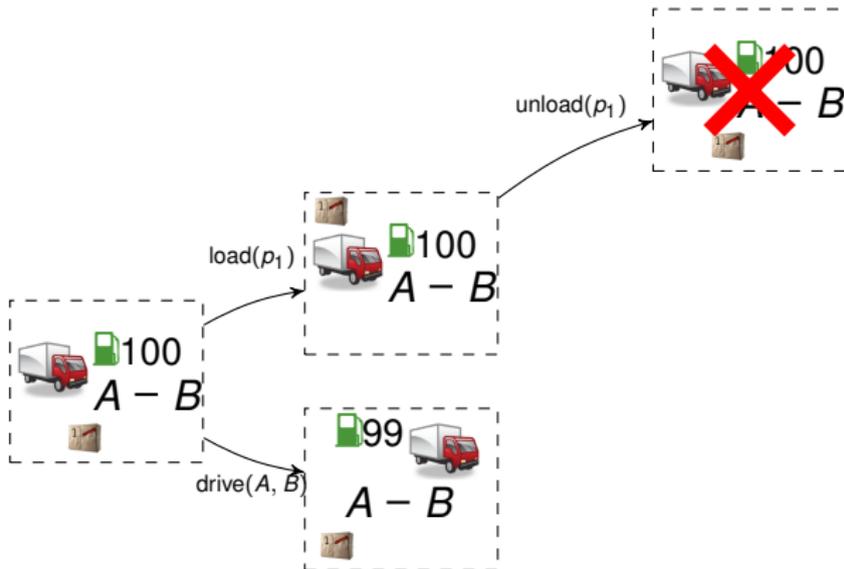
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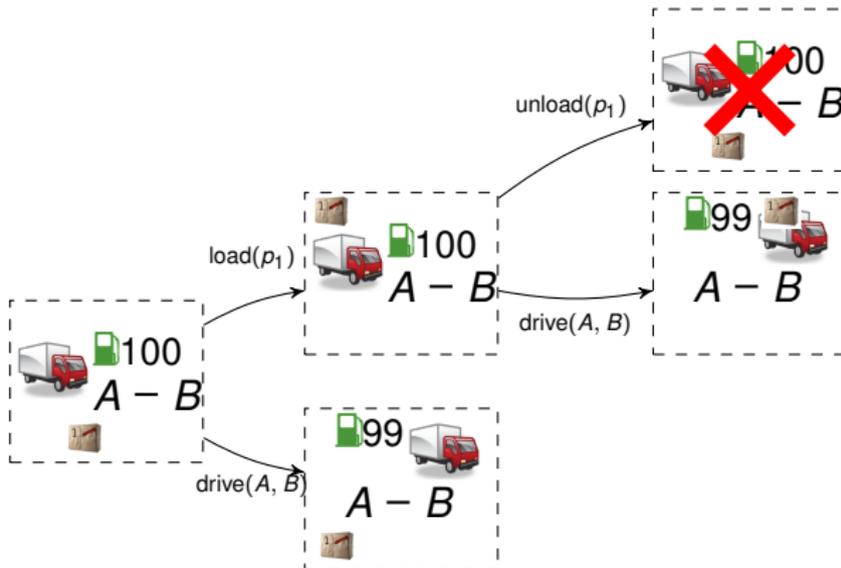
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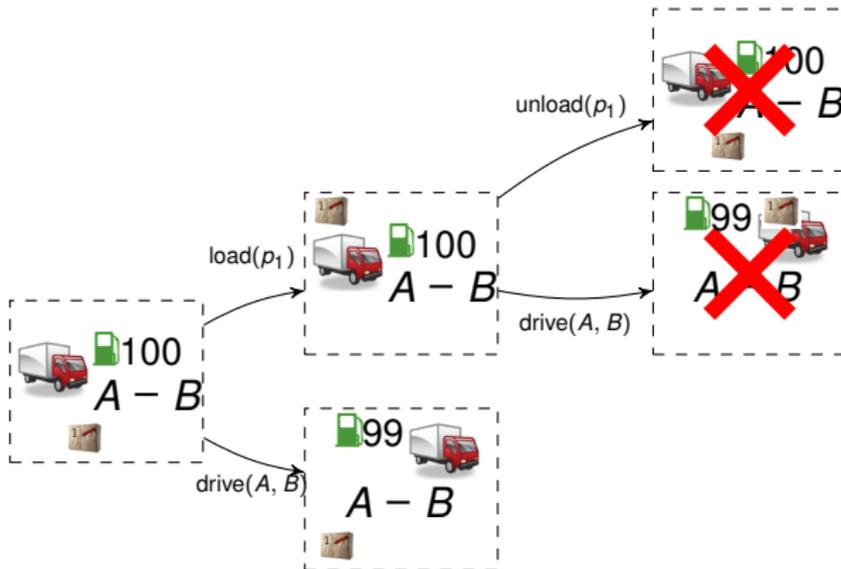
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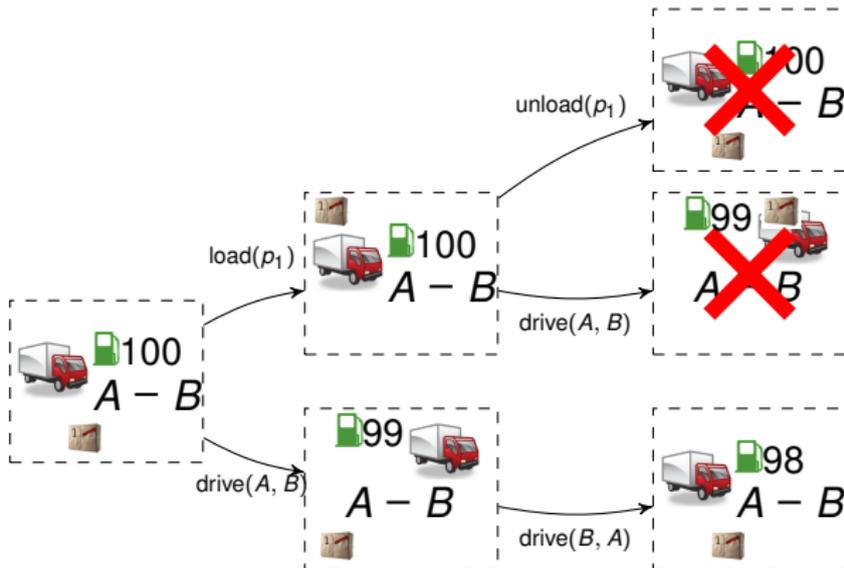
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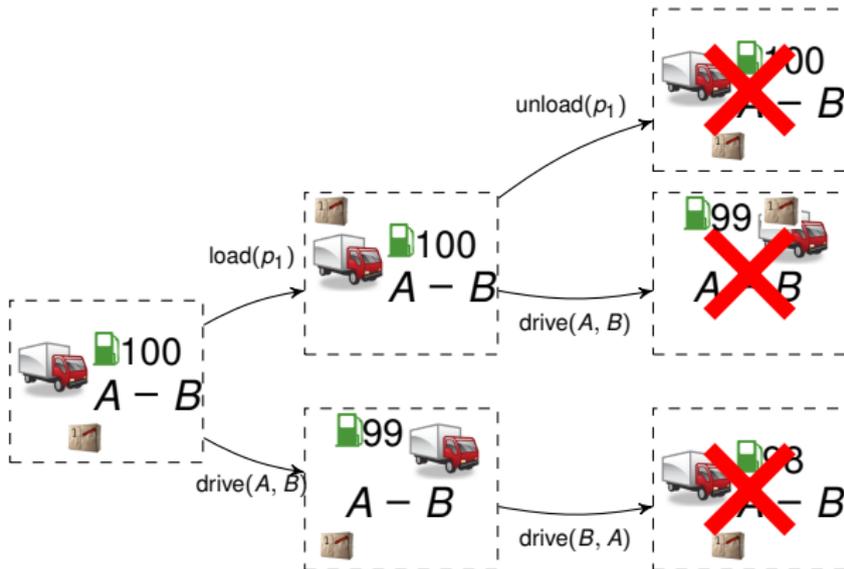
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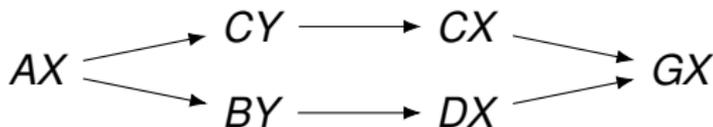
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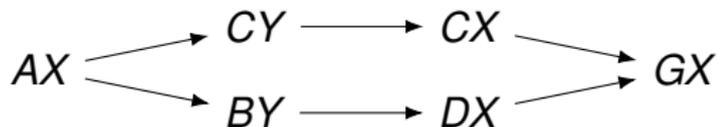


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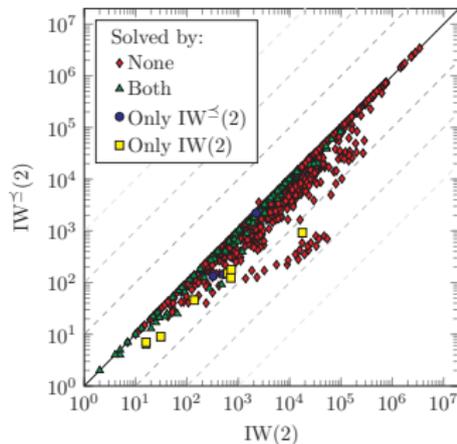
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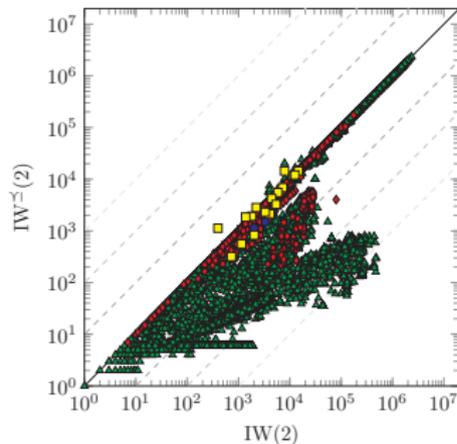


- However, there are also tasks that are solved when using  $\preceq$  but not when using  $=$

# Effective Width Analysis

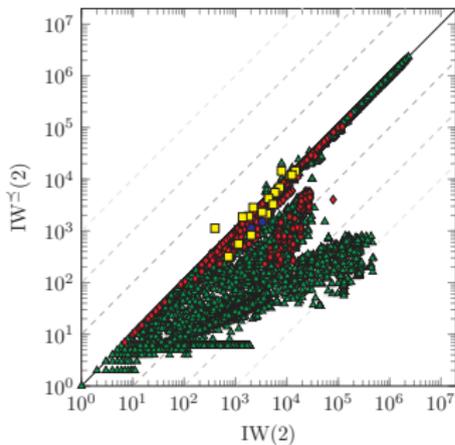
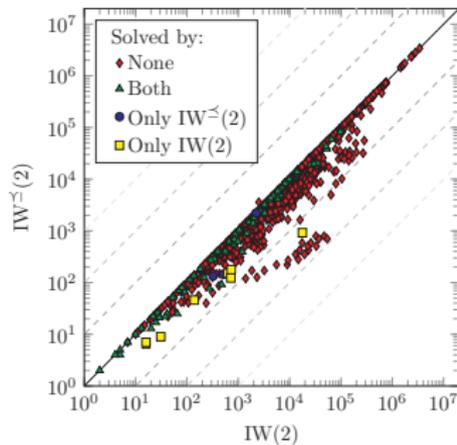


IPC Instances



1-goal instances

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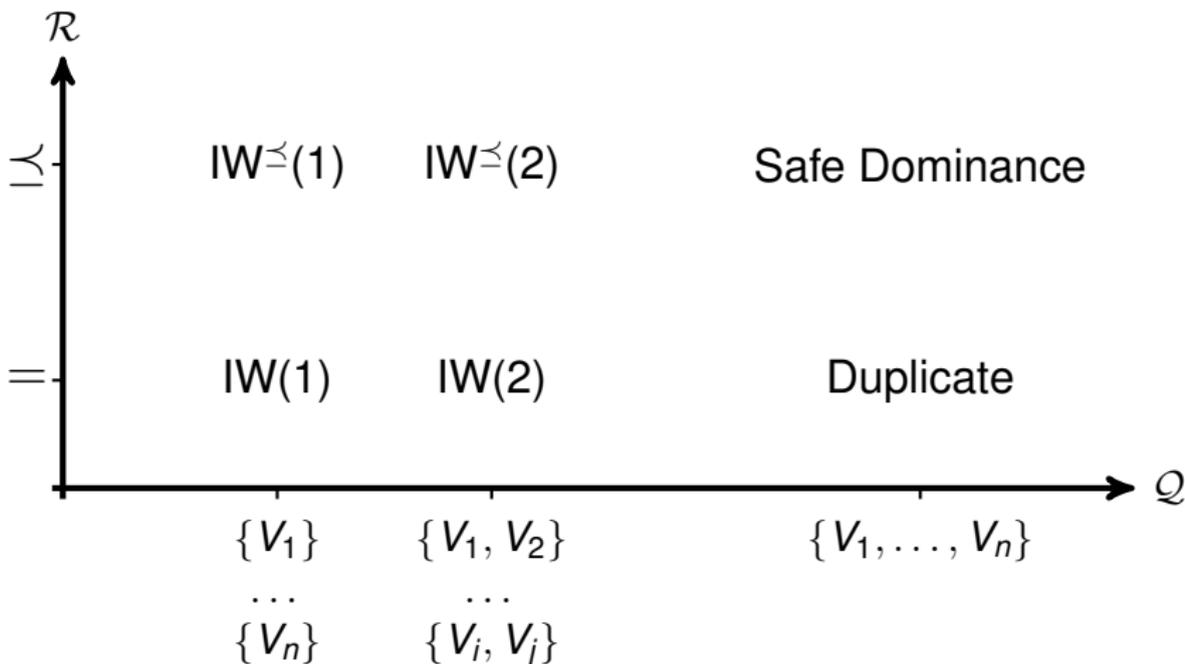
→ In practice, replacing  $=$  by  $\preceq$  increases pruning without making it more unsafe!

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A state is novel if it has a fact that no other state with **the same or lower heuristic value** has

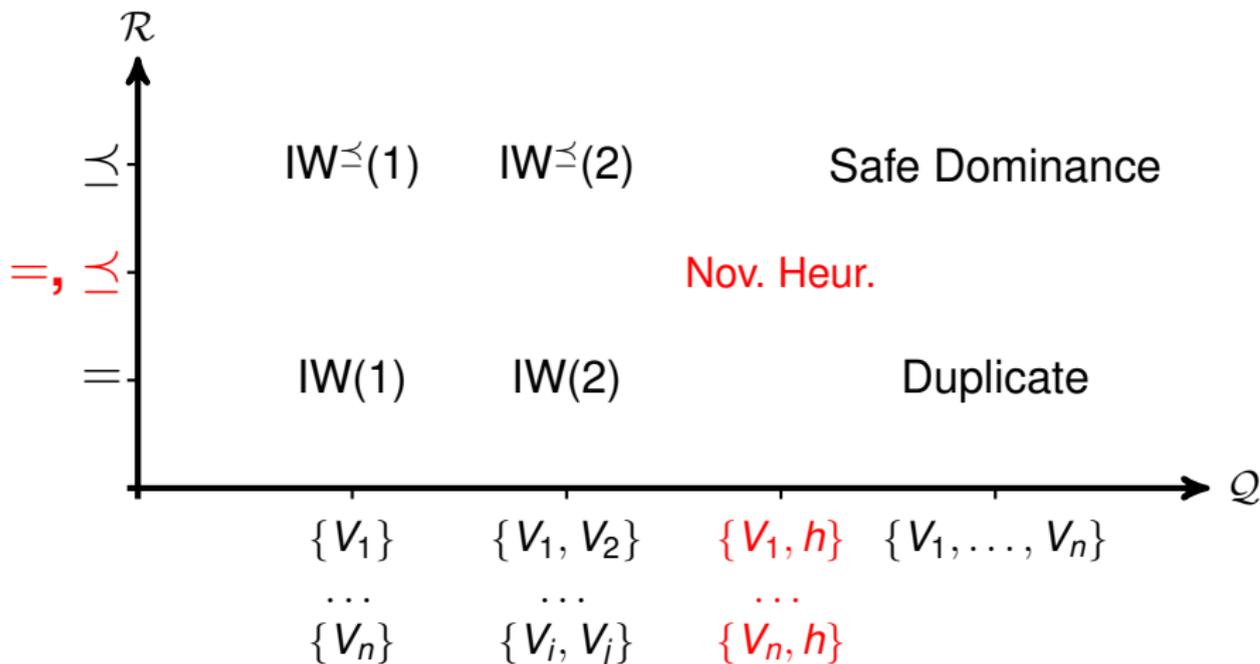
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This work: for each fact, count the number of states that have  
been seen with the same or better  $h$  value

→ Estimate the probability that the state is really dominated

## Overview of Results:

We analyze three variants:

1. Changing  $\mathcal{R}$ : = vs.  $\preceq$
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Changing  $\mathcal{R}$ : = vs.  $\preceq$

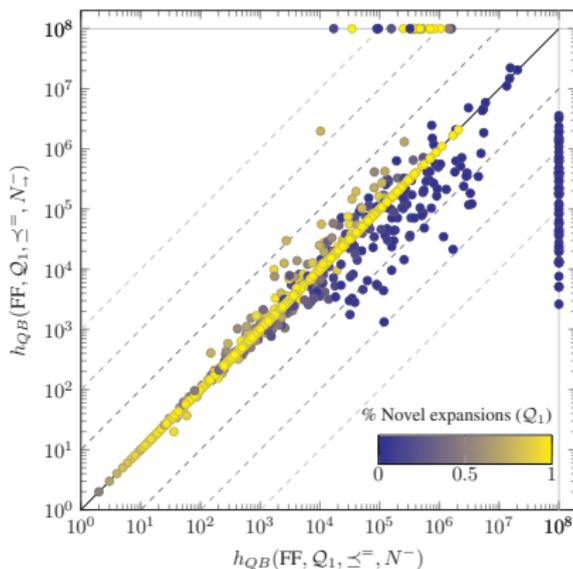
- Decreases the number of novel states
- Expansions similar to baseline
- Performance decreases due to overhead

## Changing $Q$

	$Q_1$	$Q_2$	$Q_{1,2}^{cg}$	$Q_{1,2}^{pre}$	$Q^{cg}$	$Q^{pre}$	Total
$Q_1$	–	14	8	9	8	9	1564
$Q_2$	<b>17</b>	–	6	6	8	6	1551
$Q_{1,2}^{cg}$	<b>20</b>	<b>15</b>	–	7	10	10	1609
$Q_{1,2}^{pre}$	<b>17</b>	<b>16</b>	<b>8</b>	–	9	7	1618
$Q^{cg}$	<b>20</b>	<b>20</b>	<b>15</b>	<b>13</b>	–	6	1630
$Q^{pre}$	<b>17</b>	<b>17</b>	<b>13</b>	<b>15</b>	<b>8</b>	–	<b>1634</b>

→ Best configuration in practice: choose subsets of variables that appear together in action preconditions

# Non-novel priority: $N^-$ vs. $N_{\rightarrow}^-$



- Our non-novel priority is superior to the previous one!
- But, not good synergy with changing  $Q$

# Conclusions

**Dominance**: Compare states by looking at their outgoing plans

**Novelty**: Compare states by looking at their facts

→ Our new framework on unsafe dominance generalizes both

Can we use this to devise better variants of novelty?

- $\mathcal{Q}$ : Use dominance relations in novelty
- $\mathcal{R}$ : Look at different subsets of variables
- Non-novel priority

→ Inspire new ideas to further improve novelty methods!